

**NDHU CSIE Ph.D. Qualification Examination**  
**Algorithms, Fall 2009**

1. Briefly explain these two algorithm design approaches: **divide and conquer**, **dynamic programming**. For each algorithm approach, give one example including a problem with an algorithm for the problem. What is the difference between them? (20%)
  
2. Answer the following problems about tree and heap structures:
  - (a) Draw a **binary tree** containing keys P, L, A, C, E, such that the postorder traversal visits nodes in this order: E, A, L, C, P and the inorder traversal visits nodes in order: E, L, A, P, C. (10%)
  - (b) Given a sequence S containing the elements 4, 15, 6, 3, 21, and 2, insert these elements in the given order into an empty **max-heap** data structure. Please show the final result. (10%)
  
3. Use the **master method** to give tight asymptotic bounds for the following recurrences.
  - (a)  $T(n) = 4T(n/2) + n$  (5%)
  - (b)  $T(n) = 4T(n/2) + n^2$  (5%)
  
4. Let  $(u, v)$  be a minimum-weight edge in a graph G. Show that  $(u, v)$  belongs to some minimum spanning tree to G. (10%)
  
5. The diameter of a tree  $T=(V,E)$  is the largest of all shortest-path distances in the tree. Given an efficient algorithm to compute the diameter of a tree and analyze the running time of your algorithm. (20%)
  
6. Give an algorithm that determines whether or not a given undirected graph  $G = (V, E)$  contains a cycle. Your algorithm should run in  $O(V)$  time, independent of  $|E|$ .(20%)